

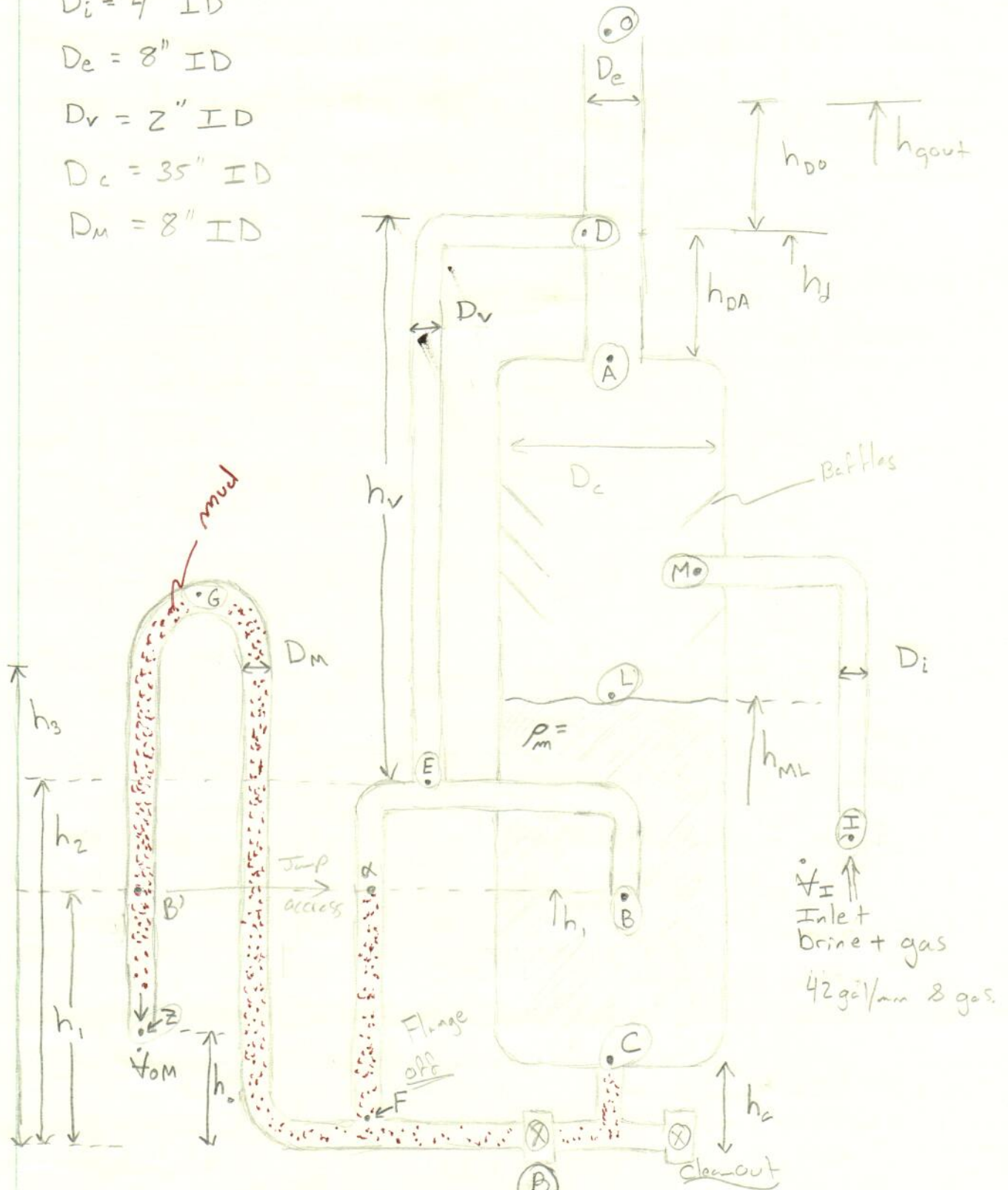
$D_i = 4'' \text{ ID}$

$D_e = 8'' \text{ ID}$

$D_v = 2'' \text{ ID}$

$D_c = 35'' \text{ ID}$

$D_m = 8'' \text{ ID}$



$h_v = 12'$

$h_1 = 29''$

$h_2 = 65''$

$h_3 = 77''$

$\rho_m = 9.5 \text{ lb/gal brine}$

$\dot{V}_{om} = 42 \text{ gpm}$

Objective: Analyze Pressures of Unit. to identify Source of air gas bubbles in the mud line.

Lets start from the Knowns and move our way thro the problem

Knowns:

Pt. O ⇒ P<sub>o</sub> = 1 atm = 1.013 × 10<sup>5</sup> Pa (Absolute → gauge is zero)

Pt. D ⇒ P<sub>D</sub> = ? we assumed @ zero in the existing design but we won't in this calculation just yet.

Pt. A ⇒ P<sub>A</sub> ≈ 100 psi = 6.89 × 10<sup>5</sup> Pa (Assume Gauge)

Pt. B ⇒ P<sub>B</sub>

Pt. C ⇒ P<sub>C</sub>

Pt. F ⇒ P<sub>F</sub>

Pt. G = P<sub>G</sub>

Pt. Z =

Ohh let's find P<sub>D</sub> with P<sub>o</sub> & P<sub>A</sub> \*



Vel > 0 Apply Bernoulli's Law

$P + \frac{1}{2}\rho v^2 + \rho gh = [constant]$

∴ Assuming V<sub>A</sub> = 0 then Apply from A to O

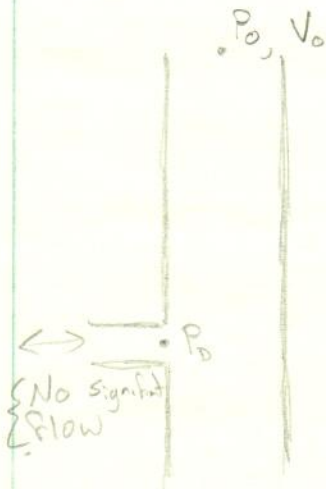
$P_A + \frac{1}{2}\rho V_A^2 + \rho g h_A = P_o + \frac{1}{2}\rho V_o^2 + \rho g h_o$

∴ In Gauge pressure P<sub>o</sub> = 0, P<sub>A</sub> = 6.89 × 10<sup>5</sup> Pa

V<sub>A</sub> = 0

$$\sqrt{\frac{P_A + \rho g(h_A - h_o)}{\frac{1}{2}\rho}} = V_o \quad \{Eq 1\}$$

now that I know the outlet velocity I should be able to go from Pt. O to Pt. D



\* Assuming No significant flow escaping gas up.  
Apply Bernoulli again

$$P_o + \frac{1}{2} \rho V_o^2 + \rho g h_o = P_D + \frac{1}{2} \rho V_D^2 + \rho g h_D$$

Solve for  $P_D$

$$P_D = \frac{1}{2} \rho (V_D^2 - V_o^2) + \rho g (h_D - h_o) \quad \{ \text{Eq 2} \}$$

this is curious because  $V_D$  should be smaller than  $V_{outlet}$  and  $h_D$  is smaller than  $h_o$  therefore it appears using  $\{ \text{Eq 2} \}$  that  $P_D$  is negative therefore creating a small vacuum in the system. I'm not 100% certain so I will continue solving the problem in its current form, and determine implications.

I'm going to assume that  $P_L = P_A$  I want to find  $P_c$

$$P_c + \frac{1}{2} \rho V_c^2 + \rho g h_c = P_L + \frac{1}{2} \rho V_L^2 + \rho g h_{ML}$$

$$V_c = 0, V_L = 0$$

$$\therefore P_c = P_L + \rho g (h_{ML} - h_c) \quad \{ \text{Eq 3} \}$$

$$\therefore P_B + \rho g h_B = P_c + \rho g h_c$$

$$P_B + \rho g h_B = P_L + \rho g h_{ML} - \rho g h_c + \rho g h_c$$

$$\therefore P_B = P_L + \rho g (h_{ML} - h_B)$$

✓ this makes sense



Now go from B to Z Ideally it should be filled with mud.

From P<sub>z</sub> to P<sub>i</sub> (@h<sub>i</sub>) we can do no problem.

$$\Sigma Eq 43 \quad P_z + \frac{1}{2} \rho V_z^2 + \rho g h_o = P_B + \frac{1}{2} \rho V_B^2 + \rho g h_i$$

A flow rate of 42 gpm of mud through 8" ID aperture and  $\rho_m = 9.5$  lb/gal brine can be converted to a velocity @  $V_z$

$$\dot{V}_{om} = 42 \frac{\text{gal}}{\text{min}} \times \frac{3.785 \text{ L}}{\text{gal}} \times \frac{1 \text{ min}}{60 \text{ sec}} \times \frac{0.001 \text{ m}^3}{1 \text{ Liter}} = 0.0026 \frac{\text{m}^3}{\text{sec}}$$

$$\dot{V}_{om} = 0.00265 \text{ m}^3/\text{sec}$$

Now convert density  $\rho_m = 9.5$  lb/gal

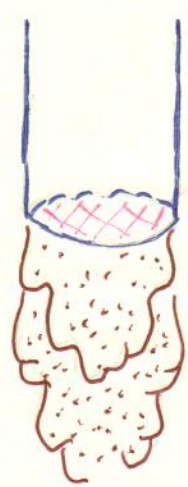
$$= \frac{9.5 \text{ lb}}{\text{gal}} \times \frac{1 \text{ gal}}{3.785 \text{ L}} \times \frac{1 \text{ L}}{0.001 \text{ m}^3} \times \frac{4.448 \text{ N}}{1 \text{ lb}}$$

$g [\text{m/s}^2]$

divide by gravity to get units in  $\text{kg/m}^3$  for density

$$\rho_m = 1139 \text{ kg/m}^3$$

← this is in the correct ballpark given that water is  $1000 \text{ kg/m}^3$



$$A_c = \pi R^2 = \pi (4 \times 0.0254)^2 \quad [\text{in} \times \frac{\text{m}}{\text{in}}]$$

$$A_c = 0.0324 \text{ m}^2$$

$$\frac{\dot{V}_{om} [\text{m}^3/\text{sec}]}{A_c [\text{m}^2]} = V_z [\text{m/sec}] = \frac{0.0026 \text{ m}^3/\text{sec}}{0.0324 \text{ m}^2}$$

$$V_z [\text{m/sec}] = 0.080 \text{ m/sec}$$

$$V_z = 8 \text{ cm/sec} \quad (\sim 3.15 \text{ inch/sec})$$

continue w/  $\Sigma E q 4 \}$

$$P_z = 1 \text{ atm open (0 gauge)}$$

$$\therefore \frac{1}{2} \rho_M V_z^2 + \rho_M g h_o = P_{B'} + \frac{1}{2} \rho V_{B'}^2 + \rho g h_i$$

assume  $V_z \approx V_{B'}$   
 $\therefore$

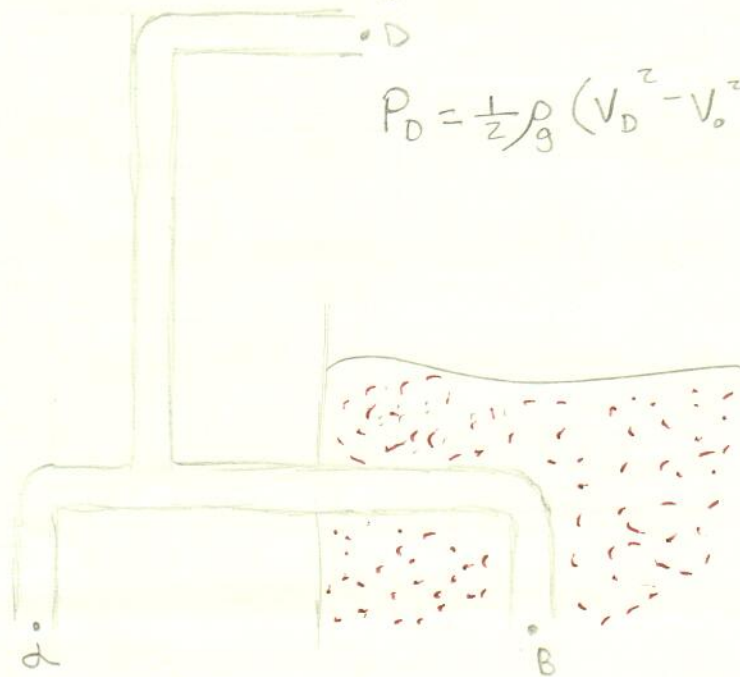
$$P_{B'} = \rho_M g (h_o - h_i) \quad \text{if } h_o > h_i, P_{B'} > 0$$

However  $h_o < h_i$ , therefore  $P_{B'}$  is negative

Now how does that compare to point  $\alpha$

Now to the Bermudas triangle

$$P_{B'} = P_\alpha$$



$$P_D = \frac{1}{2} \rho_g (V_D^2 - V_o^2) + \rho_g g (h_D - h_o)$$

$$P_\alpha = \rho_M g (h_o - h_i)$$

$$P_B = P_L + \rho_M g (h_{ML} - h_B)$$

$\uparrow P_L = P_A$  or interior pressure of vessel

Valve  $\beta$  Closed &  $h_0 < h_1$   
•  $P_E \approx \text{atm}$   
Zero

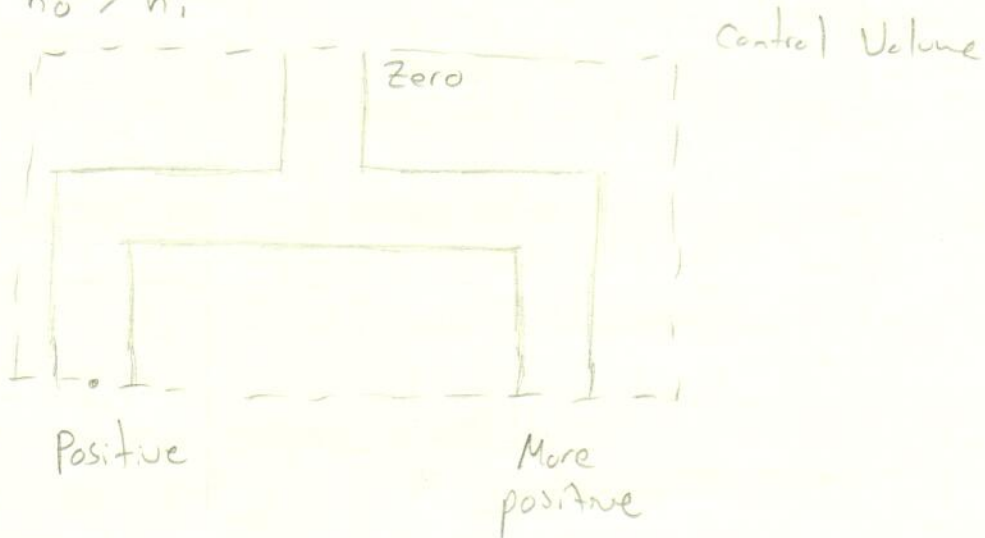
This leads me to believe that air is being sucked in from the anti-syphon Valve



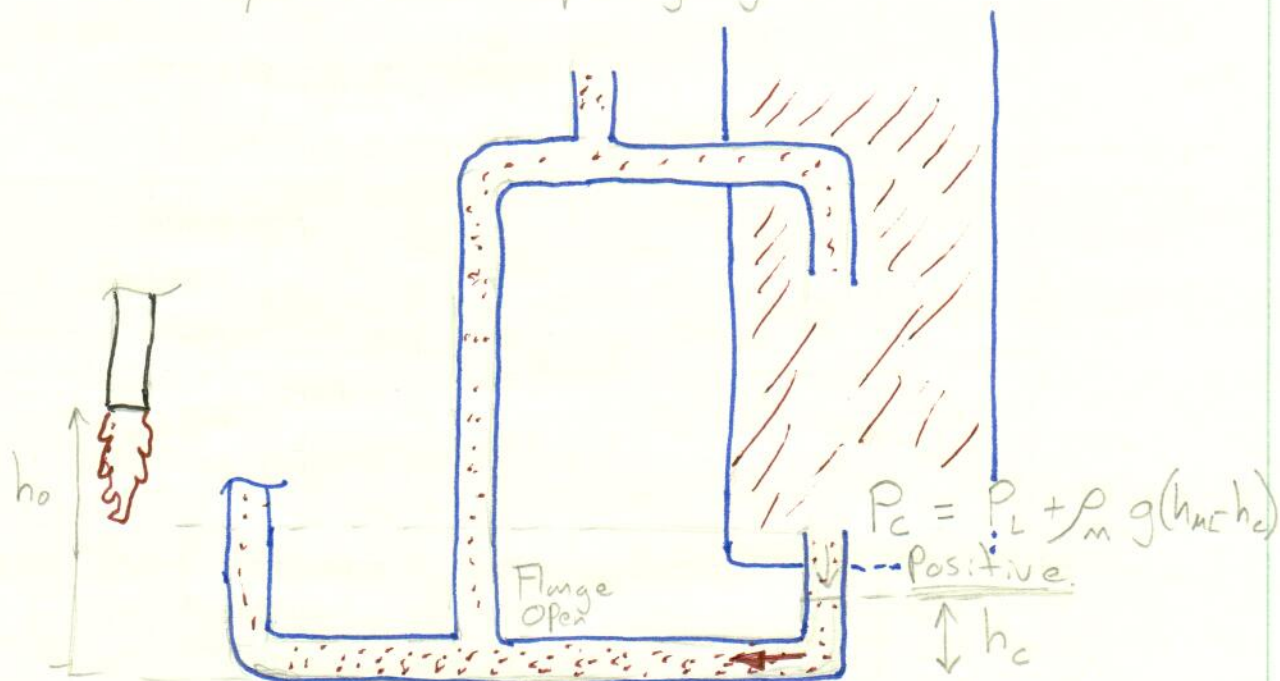
$P_B' = P_\alpha = \rho_m g (h_0 - h_1)$   
Negative

$P_B = \rho_m g (h_{mL} - h_B) + P_L$   
Positive.

Now lets still keep Valve  $\beta$  closed and make  $h_0 > h_1$



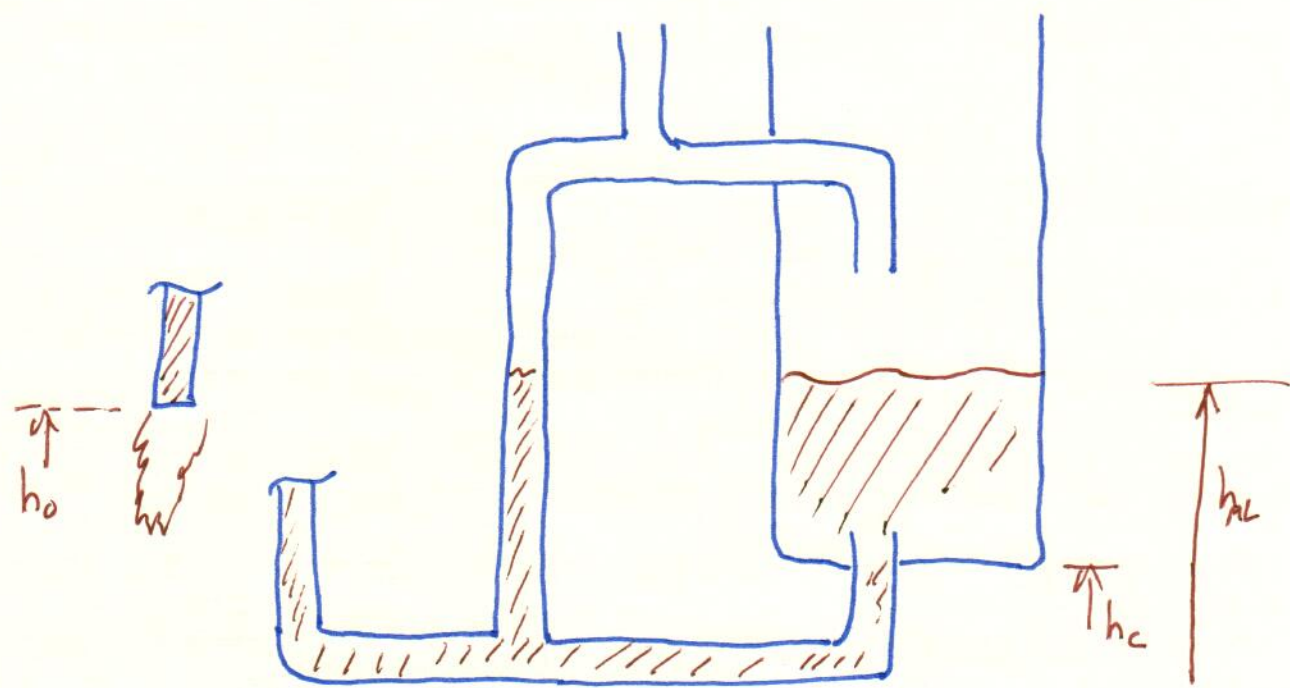
Now if we were to open Valve  $\beta$   
the  $h_c < h_o$  therefore we get to keep  
a mud layer without pulling gas



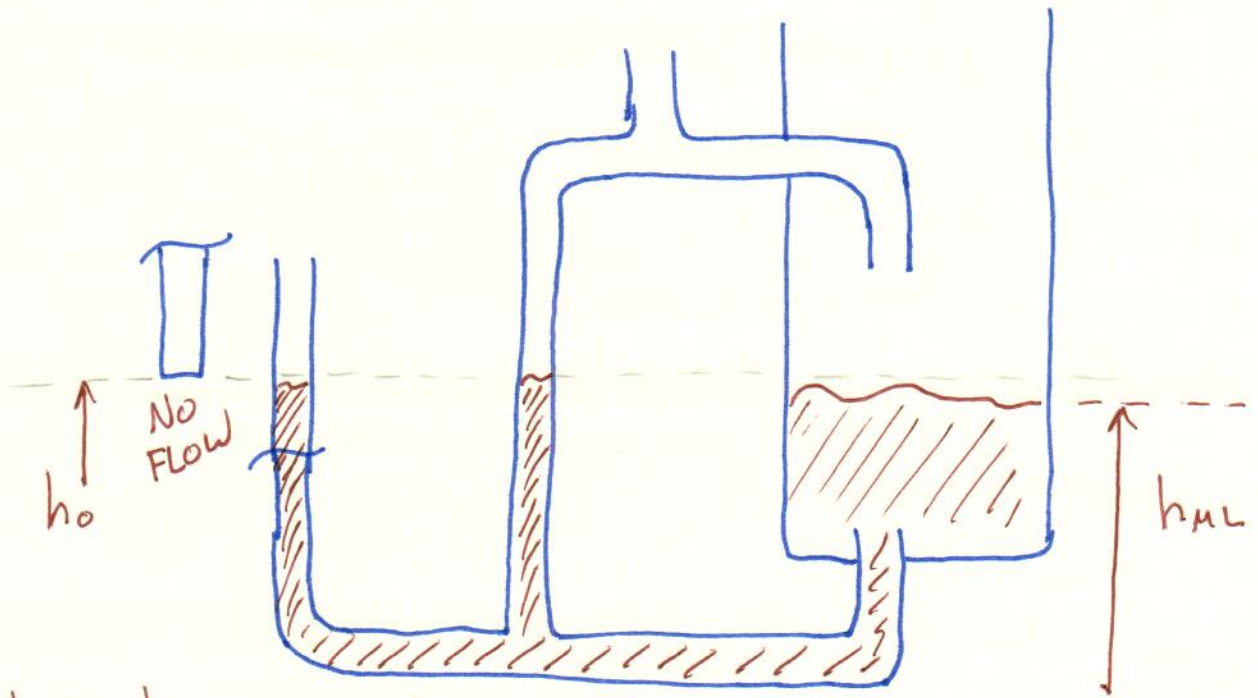
All is Happy just as long as  $h_o > h_c$   
then safety mud line is  $(h_o - h_c)$



$h_{ML} > h_o > h_c$



All is Happy just as long as  $h_{ML} > h_o$



$h_o > h_{ML}$  therefore No Flow Assumes Pressure inside separator is small but use spreadsheet to quantify.